

Probing partonic structure of a nucleon in hard electro- and neutrino-production processes

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Content:

Introduction & DVCS & TCS & DDVCS & UPC:

M. Diehl - Phys.Rept. 388 (2003),

M. Guidal, H. Moutarde, M. Vanderhaeghen - Rept.Prog.Phys. 76 (2013),

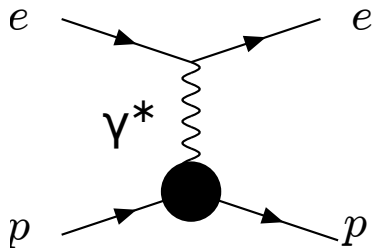
P. Kroll, H. Moutarde, F. Sabatie - Phys. Rev. D87 (2013),

E.-C. Aschenauer, S. Fazio, K. Kumericki, D. Mueller-JHEP 1309 (2013) 093

Neutrino-production of a charmed and light meson:

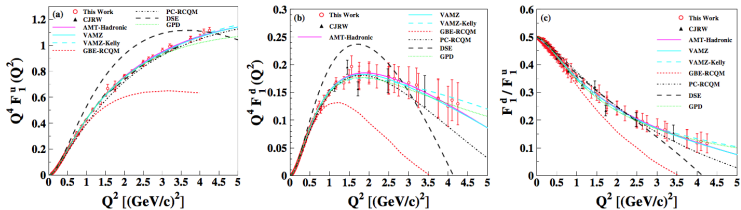
B. Pire, L.Sz. PRL 115 (2015) B. Pire, L. Sz, J. Wagner Phys. Rev. D 95 (2017)

Elastic Scattering $ep \rightarrow ep$



$$\langle p' | J^\mu(0) | p \rangle = \bar{u}(p') \left[F_1(t) \gamma^\mu + F_2(t) \frac{i\sigma^{\mu\alpha} \Delta_\alpha}{2m} \right] u(p),$$

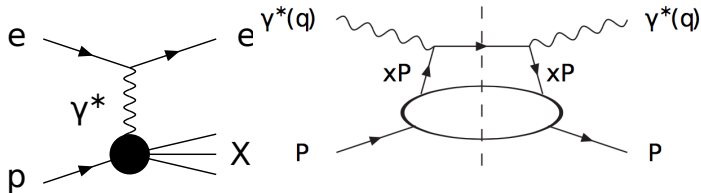
Elastic Scattering $ep \rightarrow ep$



Up- and down-quark contributions to the nucleon electromagnetic form ...

arxiv.org/pdf/1701.01662 Quattan et al

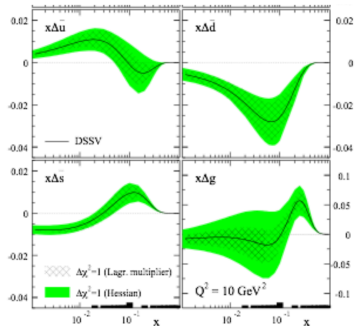
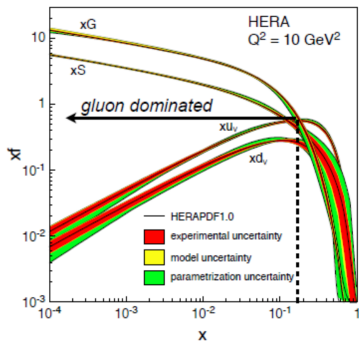
Deep Inelastic Scattering $ep \rightarrow eX$



In the Björken limit i.e. when the photon virtuality $Q^2 = -q^2$ and the squared hadronic c.m. energy $(p+q)^2$ become large, with the ratio $x_B = \frac{Q^2}{2p \cdot q}$ fixed, the cross section factorizes into a hard partonic subprocess calculable in the perturbation theory, and a parton distributions.

Collinear factorization in QCD

$$\frac{1}{2} \int \frac{dz^-}{2\pi} e^{ixP^+z^-} \langle p | \bar{q}(-\frac{1}{2}z) \gamma^+ q(\frac{1}{2}z) | p \rangle \Big|_{z^+=0, z=0} = q(x) \bar{u}(p') \gamma^+ u(p)$$

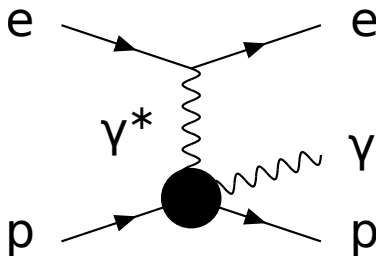


from EIC at Quarkonium 2016

<https://indico.hep.pnnl.gov/event/0/session/24/contribution/87/material/slides/0.pdf>

- Parton distributions encode the distribution of longitudinal momentum and polarization carried by quarks, antiquarks and gluons within fast moving hadron
- Still not clear how nucleons and other hadrons are built from quarks and gluons
- PDFs don't provide information about how partons are distributed in the transverse plane and ...
- about how important is the orbital angular momentum in making up the total spin of the nucleon.
- Recently - growing interest in the exclusive scattering processes, which may shed some light on these issues through the generalized parton distributions (GPD).

The simplest and best known process is Deeply Virtual Compton Scattering:
 $ep \rightarrow ep\gamma$



$$\frac{1}{2} \int \frac{dz^-}{2\pi} e^{ixP^+z^-} \langle p' | \bar{q}(-\frac{1}{2}z) \gamma^+ q(\frac{1}{2}z) | p \rangle \Big|_{z^+=0, \mathbf{z}=0}$$

$$= \frac{1}{2P^+} \left[H^q(x, \xi, t) \bar{u}(p') \gamma^+ u(p) + E^q(x, \xi, t) \bar{u}(p') \frac{i\sigma^{+\alpha} \Delta_\alpha}{2m} u(p) \right],$$

Factorization into GPDs and perturbative coefficient function - on the level of amplitude.

$$\begin{aligned} \text{DIS :} & \quad \sigma = \text{PDF} \otimes \text{partonic cross section} \\ \text{DVCS :} & \quad \mathcal{M} = \text{GPD} \otimes \text{partonic amplitude} \end{aligned}$$

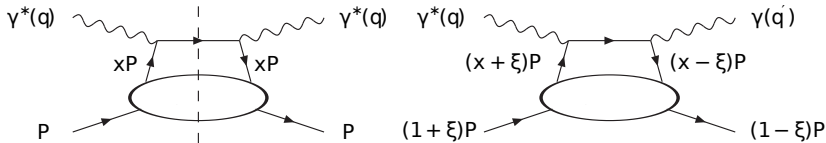


Figure: Deep Inelastic Scattering cross section is given by the imaginary part of diagram (a). Amplitude of Deeply Virtual Compton Scattering is given by diagram (b).

$$W^{\mu\nu} \sim \Im T^{\mu\nu}$$

$$P = \frac{p + p'}{2} \quad , \quad \bar{q} = \frac{q + q'}{2}$$

Generalized Bjorken variable:

$$\xi = \frac{-\bar{q}^2}{2\bar{q} \cdot P} \approx \frac{x_B}{2 - x_B} \quad , \quad x_B = \frac{Q^2}{2q \cdot p}$$

momentum transfer between proton initial and final state:

$$t = (p' - p)^2$$

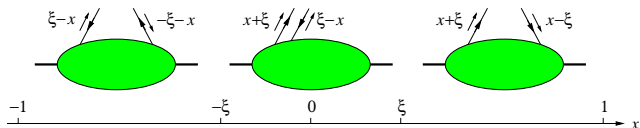
In the convenient reference frame, where P has only positive time- and z-components, and light vector are defined as:

$$v_+ = (1, 0, 0, 1) \frac{1}{\sqrt{2}} \quad , \quad v_- = (1, 0, 0, -1) \frac{1}{\sqrt{2}}$$

(-2ξ) has an interpretation of the fraction of momentum transport in "+" direction.

$$\begin{aligned}
 F^q &= \frac{1}{2} \int \frac{dz^-}{2\pi} e^{ixP^+z^-} \langle p' | \bar{q}(-\frac{1}{2}z) \gamma^+ q(\frac{1}{2}z) | p \rangle \Big|_{z^+=0, \mathbf{z}=0} \\
 &= \frac{1}{2P^+} \left[H^q(x, \xi, t) \bar{u}(p') \gamma^+ u(p) + E^q(x, \xi, t) \bar{u}(p') \frac{i\sigma^{+\alpha} \Delta_\alpha}{2m} u(p) \right], \\
 F^g &= \frac{1}{P^+} \int \frac{dz^-}{2\pi} e^{ixP^+z^-} \langle p' | G^{+\mu}(-\frac{1}{2}z) G_\mu^+(\frac{1}{2}z) | p \rangle \Big|_{z^+=0, \mathbf{z}=0} \\
 &= \frac{1}{2P^+} \left[H^g(x, \xi, t) \bar{u}(p') \gamma^+ u(p) + E^g(x, \xi, t) \bar{u}(p') \frac{i\sigma^{+\alpha} \Delta_\alpha}{2m} u(p) \right],
 \end{aligned}$$

- interpretation, ERBL, DGLAP



- Factorization scale dependence,
- Three variables x, ξ, t .

- Forward limit:

$$\begin{aligned} H^q(x, 0, 0) &= q(x), & \text{for } x > 0, \\ H^q(x, 0, 0) &= -\bar{q}(x), & \text{for } x < 0, \\ H^g(x, 0, 0) &= xg(x), \end{aligned}$$

similarly for polarized distributions and PDFs.

- Reduction to form factors:

$$\int_{-1}^1 dx H^q(x, \xi, t) = F_1^q(t), \quad \int_{-1}^1 dx E^q(x, \xi, t) = F_2^q(t),$$

where the Dirac and Pauli form factors

$$\langle p' | \bar{q}(0) \gamma^\mu q(0) | p \rangle = \bar{u}(p') \left[F_1^q(t) \gamma^\mu + F_2^q(t) \frac{i\sigma^{\mu\alpha} \Delta_\alpha}{2m} \right] u(p),$$

- Ji sum rule:

$$\lim_{t \rightarrow 0} \int_{-1}^1 dx x [H_f(x, \xi, t) + E_f(x, \xi, t)] = 2J_f$$

where J_f is fraction of the proton spin carried by quark f (including spin and orbital angular momentum).

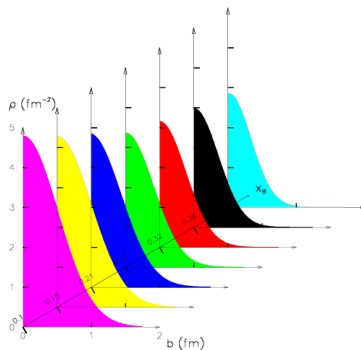
Impact parameter representation

M. Burkardt PRD 62 (2000)

At $\xi = 0 \quad \Rightarrow \quad -t = \Delta_{\perp}^2 :$

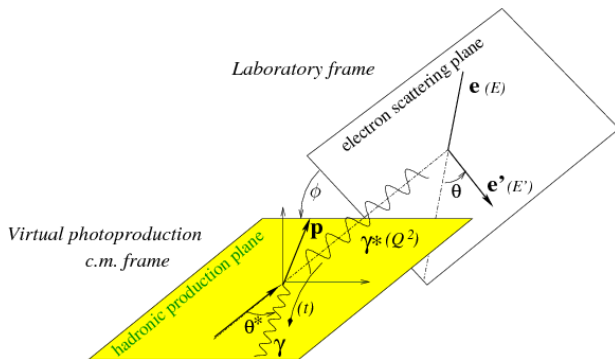
$$H(x, \mathbf{b}_{\perp}) = \int \frac{d^2 \Delta_{\perp}}{(2\pi)^2} e^{-i\mathbf{b}_{\perp} \cdot \Delta_{\perp}} H(x, 0, -\Delta_{\perp})$$

can be interpreted as probability of finding a parton with longitudinal momentum fraction x at a given \mathbf{b}_{\perp} .



- GPDs enter factorization theorems for hard **exclusive** reactions (DVCS, deeply virtual meson production, TCS etc.), in a similar manner as PDFs enter factorization theorems for **inclusive** (DIS, etc.)
- GPDs are functions of x, t, ξ, μ_F^2
- First moment of GPDs enters the Ji's sum rule for the **angular momentum** carried by partons in the nucleon,
- 2+1 imaging of nucleon,
- Deeply Virtual Compton Scattering (**DVCS**) is a golden channel for GPDs extraction,

Four variables needed to describe $ep \rightarrow ep\gamma$ at fixed beam energy. Usually : Q^2, x_B, t and ϕ :



Coefficient functions and Compton Form Factors

CFFs are the GPD dependent quantities which enter the amplitudes. They are defined through relations:

$$\mathcal{A}^{\mu\nu}(\xi, t) = -e^2 \frac{1}{(P+P')^+} \bar{u}(P') \left[g_T^{\mu\nu} \left(\mathcal{H}(\xi, t) \gamma^+ + \mathcal{E}(\xi, t) \frac{i\sigma^{+\rho} \Delta_\rho}{2M} \right) + i\epsilon_T^{\mu\nu} \left(\tilde{\mathcal{H}}(\xi, t) \gamma^+ \gamma_5 + \tilde{\mathcal{E}}(\xi, t) \frac{\Delta^+ \gamma_5}{2M} \right) \right] u(P),$$

,where:

$$\mathcal{H}(\xi, t) = + \int_{-1}^1 dx \left(\sum_q T^q(x, \xi) H^q(x, \xi, t) + T^g(x, \xi) H^g(x, \xi, t) \right)$$

GPDs enter through convolutions! At LO in α_S :

$$DVCS T^q = -e_q^2 \frac{1}{x + \xi - i\epsilon} - (x \rightarrow -x)$$

$$DVCS \text{Re}(\mathcal{H}) \sim P \int \frac{1}{x + \xi} H^q(x, \xi, t), \quad DVCS \text{Im}(\mathcal{H}) \sim i\pi H^q(\xi, \xi, t)$$

Figure 12 from Michel Guidal et al 2013 Rep. Prog. Phys. 76 066202

$$\sigma(ep \rightarrow ep\gamma) \propto \left[\text{DVCS} + \text{BH} \right]^2$$

The diagram shows the cross-section $\sigma(ep \rightarrow ep\gamma) \propto \left[\text{DVCS} + \text{BH} \right]^2$. The DVCS term is represented by a single diagram where an incoming electron (e) and proton (p) interact via a virtual photon (γ^*) with a target (black circle), resulting in an outgoing electron (e'), proton (p'), and real photon (γ). The BH term is represented by a bracketed group of three diagrams: 1) a proton emits a real photon (γ) before interacting with the electron via a virtual photon (γ^*); 2) an electron emits a real photon (γ) before interacting with the proton via a virtual photon (γ^*); 3) the electron and proton interact via a virtual photon (γ^*), and then the electron emits a real photon (γ).

The $lp \rightarrow lp\gamma$ cross section on an unpolarized target for a given beam charge, e_l in units of the positron charge and beam helicity $h_l/2$ can be written as :

$$d\sigma^{h_l, e_l}(\phi) = d\sigma_{UU}(\phi) [1 + h_l A_{LU, DVCS}(\phi) + e_l h_l A_{LU, I}(\phi) + e_l A_C(\phi)] ,$$

If both longitudinally polarized positively and negatively charged beams are available (HERMES):

$$A_C(\phi) = \frac{1}{4d\sigma_{UU}(\phi)} \left[(d\sigma^{\rightarrow\rightarrow} + d\sigma^{\leftarrow\leftarrow}) - (d\sigma^{\rightarrow\leftarrow} + d\sigma^{\leftarrow\rightarrow}) \right] . \quad (1)$$

$$A_{LU, I}(\phi) = \frac{1}{4d\sigma_{UU}(\phi)} \left[(d\sigma^{\rightarrow\rightarrow} - d\sigma^{\leftarrow\leftarrow}) - (d\sigma^{\rightarrow\leftarrow} - d\sigma^{\leftarrow\rightarrow}) \right] , \quad (2)$$

$$A_{LU, DVCS}(\phi) = \frac{1}{4d\sigma_{UU}(\phi)} \left[(d\sigma^{\rightarrow\rightarrow} - d\sigma^{\leftarrow\leftarrow}) + (d\sigma^{\rightarrow\leftarrow} - d\sigma^{\leftarrow\rightarrow}) \right] . \quad (3)$$

If an experiment only has access to one value of e_l such as in Jefferson Lab, one can only measure the beam spin asymmetry $A_{LU}^{e_l}$

$$A_{LU}^{e_l}(\phi) = \frac{d\sigma^{\rightarrow\rightarrow} - d\sigma^{\leftarrow\leftarrow}}{d\sigma^{\rightarrow\rightarrow} + d\sigma^{\leftarrow\leftarrow}} , \quad (4)$$

Target longitudinal spin asymmetry which reads :

$$A_{\text{UL}}^{e_l}(\phi) = \frac{[d\sigma^{\leftarrow\Rightarrow} + d\sigma^{\rightarrow\Rightarrow}] - [d\sigma^{\leftarrow\Leftarrow} + d\sigma^{\rightarrow\Leftarrow}]}{[d\sigma^{\leftarrow\Rightarrow} + d\sigma^{\rightarrow\Rightarrow}] + [d\sigma^{\leftarrow\Leftarrow} + d\sigma^{\rightarrow\Leftarrow}]}, \quad (5)$$

where the double arrows \Leftarrow (\Rightarrow) refer to the target polarization state parallel (anti-parallel) to the beam momentum. The double longitudinal target spin asymmetry is defined in a similar fashion :

$$A_{\text{LL}}^{e_l}(\phi) = \frac{[d\sigma^{\rightarrow\Rightarrow} + d\sigma^{\leftarrow\Leftarrow}] - [d\sigma^{\leftarrow\Rightarrow} + d\sigma^{\rightarrow\Leftarrow}]}{[d\sigma^{\rightarrow\Rightarrow} + d\sigma^{\leftarrow\Leftarrow}] + [d\sigma^{\leftarrow\Rightarrow} + d\sigma^{\rightarrow\Leftarrow}]}, \quad (6)$$

The HERMES collaboration also had access to a transversally polarized target with both electrons and positrons:

$$A_{\text{UT,I}}(\phi, \phi_S) = \frac{d\sigma^+(\phi, \phi_S) + d\sigma^+(\phi, \phi_S + \pi) - d\sigma^-(\phi, \phi_S) - d\sigma^-(\phi, \phi_S + \pi)}{d\sigma^+(\phi, \phi_S) - d\sigma^+(\phi, \phi_S + \pi) + d\sigma^-(\phi, \phi_S) - d\sigma^-(\phi, \phi_S + \pi)},$$

$$A_{\text{UT,DVCS}}(\phi, \phi_S) = \frac{d\sigma^+(\phi, \phi_S) - d\sigma^+(\phi, \phi_S + \pi) - d\sigma^-(\phi, \phi_S) + d\sigma^-(\phi, \phi_S + \pi)}{d\sigma^+(\phi, \phi_S) - d\sigma^+(\phi, \phi_S + \pi) + d\sigma^-(\phi, \phi_S) - d\sigma^-(\phi, \phi_S + \pi)}.$$

$$\begin{aligned}
 A_C^{\cos \phi} &\propto \operatorname{Re} \left[F_1 \mathcal{H} + \xi(F_1 + F_2) \tilde{\mathcal{H}} - \frac{t}{4m^2} F_2 \mathcal{E} \right], \\
 A_{LU,I}^{\sin \phi} &\propto \operatorname{Im} \left[F_1 \mathcal{H} + \xi(F_1 + F_2) \tilde{\mathcal{H}} - \frac{t}{4m^2} F_2 \mathcal{E} \right], \\
 A_{UL,I}^{\sin \phi} &\propto \operatorname{Im} \left[\xi(F_1 + F_2) \left(\mathcal{H} + \frac{\xi}{1+\xi} \mathcal{E} \right) + F_1 \tilde{\mathcal{H}} - \xi \left(\frac{\xi}{1+\xi} F_1 + \frac{t}{4M^2} F_2 \right) \tilde{\mathcal{E}} \right], \\
 A_{LL,I}^{\cos \phi} &\propto \operatorname{Re} \left[\xi(F_1 + F_2) \left(\mathcal{H} + \frac{\xi}{1+\xi} \mathcal{E} \right) + F_1 \tilde{\mathcal{H}} - \xi \left(\frac{\xi}{1+\xi} F_1 + \frac{t}{4M^2} F_2 \right) \tilde{\mathcal{E}} \right], \\
 A_{LL,DVCS}^{\cos(0\phi)} &\propto \operatorname{Re} \left[4(1 - \xi^2) (\mathcal{H} \tilde{\mathcal{H}}^* + \tilde{\mathcal{H}} \mathcal{H}^*) - 4\xi^2 (\mathcal{H} \tilde{\mathcal{E}}^* + \tilde{\mathcal{E}} \mathcal{H}^* + \tilde{\mathcal{H}} \mathcal{E}^* + \mathcal{E} \tilde{\mathcal{H}}^*) \right. \\
 &\quad \left. - 4\xi \left(\frac{\xi^2}{1+\xi} + \frac{t}{4M^2} \right) (\mathcal{E} \tilde{\mathcal{E}}^* + \tilde{\mathcal{E}} \mathcal{E}^*) \right], \\
 A_{UT,DVCS}^{\sin(\phi - \phi_s)} &\propto \left[\operatorname{Im} (\mathcal{H} \mathcal{E}^*) - \xi \operatorname{Im} (\tilde{\mathcal{H}} \tilde{\mathcal{E}}^*) \right], \\
 A_{UT,I}^{\sin(\phi - \phi_s) \cos \phi} &\propto \operatorname{Im} \left[-\frac{t}{4M^2} (F_2 \mathcal{H} - F_1 \mathcal{E}) + \xi^2 \left(F_1 + \frac{t}{4M^2} F_2 \right) (\mathcal{H} + \mathcal{E}) \right. \\
 &\quad \left. - \xi^2 (F_1 + F_2) \left(\tilde{\mathcal{H}} + \frac{t}{4M^2} \tilde{\mathcal{E}} \right) \right]. \tag{7}
 \end{aligned}$$

Experiment	Observable	Normalized CFF dependence
HERMES	$A_C^{\cos 0\phi}$	$\text{Re}\mathcal{H} + 0.06\text{Re}\mathcal{E} + 0.24\text{Re}\tilde{\mathcal{H}}$
	$A_C^{\cos \phi}$	$\text{Re}\mathcal{H} + 0.05\text{Re}\mathcal{E} + 0.15\text{Re}\tilde{\mathcal{H}}$
	$A_{LU,I}^{\sin \phi}$	$\text{Im}\mathcal{H} + 0.05\text{Im}\mathcal{E} + 0.12\text{Im}\tilde{\mathcal{H}}$
	$A_{UL}^{+, \sin \phi}$	$\text{Im}\tilde{\mathcal{H}} + 0.10\text{Im}\mathcal{H} + 0.01\text{Im}\mathcal{E}$
	$A_{UL}^{+, \sin 2\phi}$	$\text{Im}\tilde{\mathcal{H}} - 0.97\text{Im}\mathcal{H} + 0.49\text{Im}\mathcal{E} - 0.03\text{Im}\tilde{\mathcal{E}}$
	$A_{LL}^{+, \cos 0\phi}$	$1 + 0.05\text{Re}\tilde{\mathcal{H}} + 0.01\text{Re}\mathcal{H}$
	$A_{LL}^{+, \cos \phi}$	$1 + 0.79\text{Re}\tilde{\mathcal{H}} + 0.11\text{Im}\mathcal{H}$
	$A_{UT,DVCS}^{\sin(\phi-\phi_S)}$	$\text{Im}\mathcal{H}\text{Re}\mathcal{E} - \text{Im}\mathcal{E}\text{Re}\mathcal{H}$
	$A_{UT,I}^{\sin(\phi-\phi_S)\cos\phi}$	$\text{Im}\mathcal{H} - 0.56\text{Im}\mathcal{E} - 0.12\text{Im}\tilde{\mathcal{H}}$
CLAS	$A_{LU}^-, \sin \phi$	$\text{Im}\mathcal{H} + 0.06\text{Im}\mathcal{E} + 0.21\text{Im}\tilde{\mathcal{H}}$
	$A_{UL}^-, \sin \phi$	$\text{Im}\tilde{\mathcal{H}} + 0.12\text{Im}\mathcal{H} + 0.04\text{Im}\mathcal{E}$
	$A_{UL}^-, \sin 2\phi$	$\text{Im}\tilde{\mathcal{H}} - 0.79\text{Im}\mathcal{H} + 0.30\text{Im}\mathcal{E} - 0.05\text{Im}\tilde{\mathcal{E}}$
HALL A	$\Delta\sigma^{\sin \phi}$	$\text{Im}\mathcal{H} + 0.07\text{Im}\mathcal{E} + 0.47\text{Im}\tilde{\mathcal{H}}$
	$\sigma^{\cos 0\phi}$	$1 + 0.05\text{Re}\mathcal{H} + 0.007\mathcal{H}\mathcal{H}^*$
	$\sigma^{\cos \phi}$	$1 + 0.12\text{Re}\mathcal{H} + 0.05\text{Re}\tilde{\mathcal{H}}$
HERA	σ_{DVCS}	$\mathcal{H}\mathcal{H}^* + 0.09\mathcal{E}\mathcal{E}^* + \tilde{\mathcal{H}}\tilde{\mathcal{H}}^*$

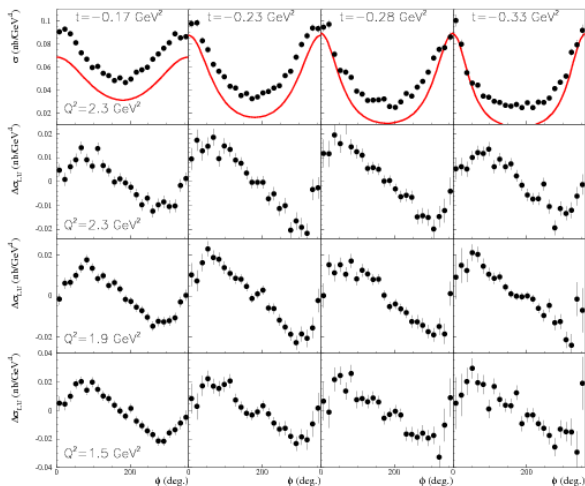
$E_e = 5.75 \text{ GeV}$, $x_B = 0.36$


Figure: HALL A data. Red curve - pure BH contribution.

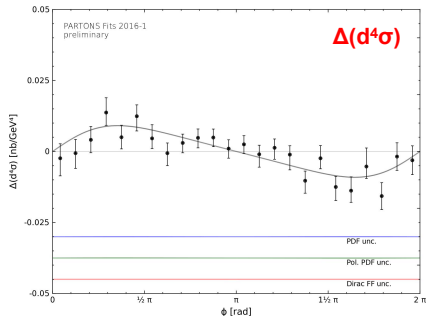
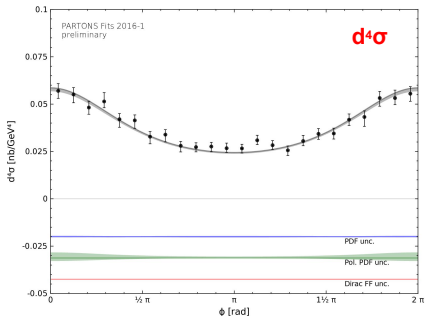
Topic for another seminar...

- A lot of data, but not enough to fit 4 GPDs (function of 3 variables) for every quark flavour ... and gluons
- GPDs must satisfy certain principles
- Few models on the market (Goloskokov-Kroll, VGG, Kumericki-Mueller ...), most of them describe data well (small problems with Hall A), only one describes all data - including small x .
- still much more data needed to determine GPDs (mostly the imaginary part of CFF H determined)
- PARTONS - modern platform devoted to study GPDs (Herve Moutarde, Saclay)

RESULTS

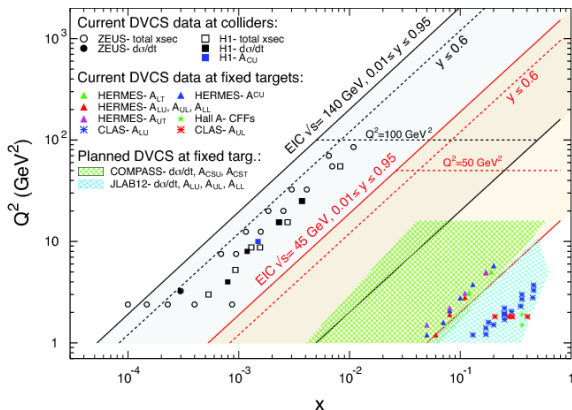
Hall A: X2 kinematics: $d^4\sigma$ and $\Delta(d^4\sigma)$
 @ $x_B = 0.39$, $t = -0.23 \text{ GeV}^2$, $Q^2 = 2.1 \text{ GeV}^2$, $E = 5.8 \text{ GeV}$

 0.68 c.l.

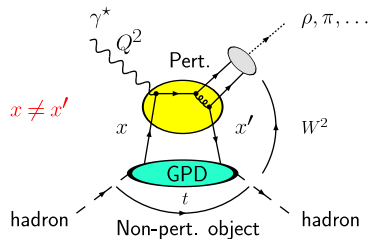
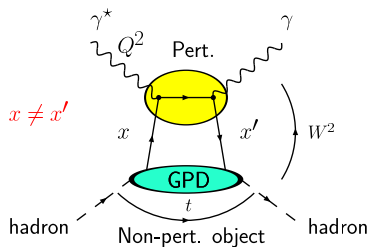


Good description of experimental data

- JLAB - 12 GeV . Plans for Hall A and CLAS to measure beam spin and target spin asymmetries with much higher luminosity, smaller x_B and higher Q^2 . Also CLAS plan to measure DVCS on neutron - necessary to make GPD flavour separation.
- COMPASS - recoil detector to ensure exclusivity - plans to measure mixed charge-spin asymmetries with 160GeV muon beam.
- EIC (!)



- Difficult: exclusivity, 3 variables, GPD enter through convolutions, only $\text{GPD}(\xi, \xi, t)$ accesible through DVCS at LO!
- universality,
- flavour separation,



- Meson production - additional information (and difficulties),

So, in addition to spacelike DVCS ...

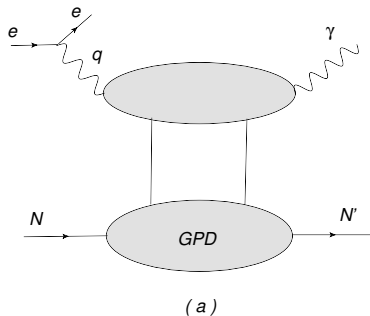


Figure: Deeply Virtual Compton Scattering (DVCS) : $lN \rightarrow l'N'\gamma$

we can also study **timelike** DVCS

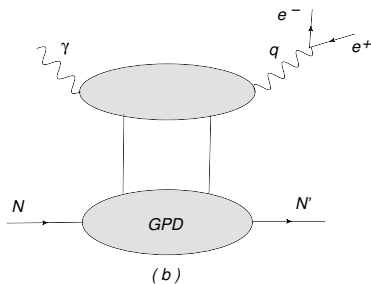


Figure: Timelike Compton Scattering (**TCS**): $l^- N \rightarrow l^- N' l'^+ l'^-$

Why **TCS**:

- universality of the GPDs
- another source for GPDs (special sensitivity on real part of GPD H),
- spacelike-timelike crossing,
- first step towards DDCVS,

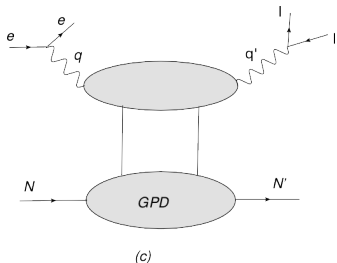


Figure: Double Deeply Virtual Compton Scattering (**DDVCS**): $\gamma N \rightarrow l+l^- N'$

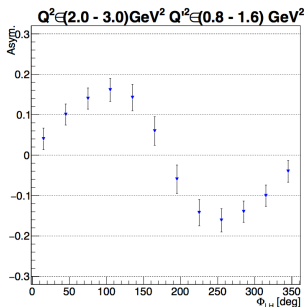
$$\gamma^*(q_{in})N(p) \rightarrow \gamma^*(q_{out})N'(p')$$

variables, describing the processes of interest in this generalized Bjorken limit, are the **scaling variable** ξ and **skewness** $\eta > 0$:

$$\xi = -\frac{q_{out}^2 + q_{in}^2}{q_{out}^2 - q_{in}^2}\eta, \quad \eta = \frac{q_{out}^2 - q_{in}^2}{(p + p') \cdot (q_{in} + q_{out})}.$$

- DDVCS: $q_{in}^2 < 0$, $q_{out}^2 > 0$, $\eta \neq \xi$
- DVCS: $q_{in}^2 < 0$, $q_{out}^2 = 0$, $\eta = \xi > 0$
- TCS: $q_{in}^2 = 0$, $q_{out}^2 > 0$, $\eta = -\xi > 0$

A DDVCS experiment using a modified CLAS12 detector and 11 GeV electron beam in Hall-B was introduced as a letter of intent to Jefferson Lab PAC44



Projected statistical uncertainties, based on Bethe-Heitler cross section, on the beam spin asymmetry calculated from the VGG model, for one example of Q'^2 bin in the proposed CLAS12 DDVCS experiment

CFFs are the GPD dependent quantities which enter the amplitudes and now depend on two variables: skewness ξ and skewness η .

$$\mathcal{A}^{\mu\nu}(\xi, \eta, t) = -e^2 \frac{1}{(P + P')_+} \bar{u}(P') \left[g_T^{\mu\nu} \left(\mathcal{H}(\xi, \eta, t) \gamma^+ + \mathcal{E}(\xi, \eta, t) \frac{i\sigma^{+\rho} \Delta_\rho}{2M} \right) + i\epsilon_T^{\mu\nu} \left(\tilde{\mathcal{H}}(\xi, \eta, t) \gamma^+ \gamma_5 + \tilde{\mathcal{E}}(\xi, \eta, t) \frac{\Delta^+ \gamma_5}{2M} \right) \right] u(P),$$

,where:

$$\mathcal{H}(\xi, \eta, t) = + \int_{-1}^1 dx \left(\sum_q T^q(x, \xi, \eta) H^q(x, \eta, t) + T^g(x, \xi, \eta) H^g(x, \eta, t) \right)$$

$$\tilde{\mathcal{H}}(\xi, \eta, t) = - \int_{-1}^1 dx \left(\sum_q \tilde{T}^q(x, \xi, \eta) \tilde{H}^q(x, \eta, t) + \tilde{T}^g(x, \xi, \eta) \tilde{H}^g(x, \eta, t) \right).$$

- DVCS vs TCS

$$\begin{aligned}
 DVCS T^q &= -e_q^2 \frac{1}{x+\eta-i\epsilon} - (x \rightarrow -x) = (TCS T^q)^* \\
 DVCS \tilde{T}^q &= -e_q^2 \frac{1}{x+\eta-i\epsilon} + (x \rightarrow -x) = -(TCS \tilde{T}^q)^*
 \end{aligned}$$

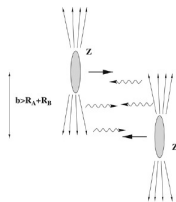
$$DVCS Re(\mathcal{H}) \sim P \int \frac{1}{x \pm \eta} H^q(x, \eta, t), \quad DVCS Im(\mathcal{H}) \sim i\pi H^q(\pm\eta, \eta, t)$$

- DDVCS

$$\begin{aligned}
 DDVCS T^q &= -e_q^2 \frac{1}{x+\xi-i\epsilon} - (x \rightarrow -x) \\
 DDVCS Re(\mathcal{H}) &\sim P \int \frac{1}{x \pm \xi} H^q(x, \eta, t), \quad DDVCS Im(\mathcal{H}) \sim i\pi H^q(\pm\xi, \eta, t)
 \end{aligned}$$

But this is only true at LO. At NLO all GPDs hidden in the convolutions.

Ultraperipheral collisions



$$\sigma = \int \frac{dn(k)}{dk} \sigma_{\gamma p}(k) dk$$

$\sigma_{\gamma p}(k)$ is the cross section for the $\gamma p \rightarrow pl^+l^-$ process and k is the γ 's energy, and $\frac{dn(k)}{dk}$ is an equivalent photon flux.

$$\frac{dn}{dk} = \frac{2Z^2 \alpha_{EM}}{\pi k} \left[\omega^{pA} K_0(\omega^{pA}) K_1(\omega^{pA}) - \frac{\omega^{pA^2}}{2} \left(K_1^2(\omega^{pA}) - K_0^2(\omega^{pA}) \right) \right] \quad (8)$$

The TCS differential cross section at UPC

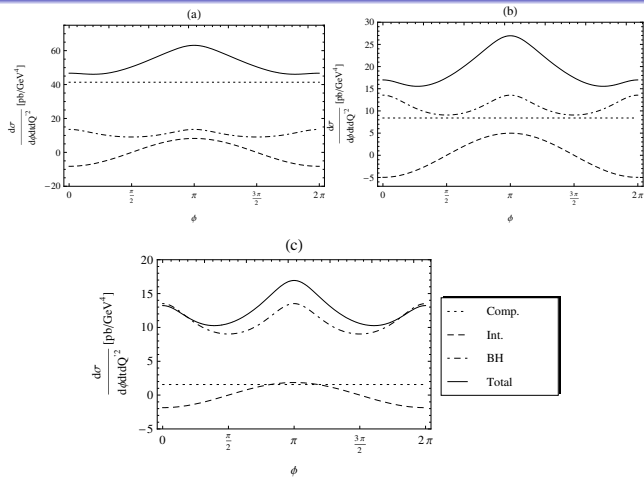


Figure: The differential cross sections (solid lines) for $t = -0.2 \text{ GeV}^2$, $Q'^2 = 5 \text{ GeV}^2$ and integrated over $\theta = [\pi/4, 3\pi/4]$, as a function of φ , for $s = 10^7 \text{ GeV}^2$ (a), $s = 10^5 \text{ GeV}^2$ (b), $s = 10^3 \text{ GeV}^2$ (c) with $\mu_F^2 = 5 \text{ GeV}^2$. We also display the Compton (dotted), Bethe-Heitler (dash-dotted) and Interference (dashed) contributions.

Gluon GPDs in the UPC production of heavy mesons

Work in progress with D.Yu.Ivanov and J. Wagner

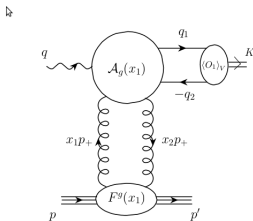


Figure 1: Kinematics of heavy vector meson photoproduction.

D. Yu. Ivanov , A. Schafer , L. Szymanowski and G. Krasnikov - **Eur.Phys.J. C34 (2004) 297-316**

The amplitude \mathcal{M} is given by factorization formula:

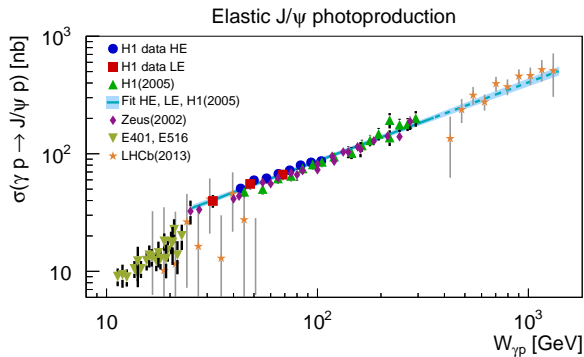
$$\mathcal{M} \sim \left(\frac{\langle O_1 \rangle_V}{m^3} \right)^{1/2} \int_{-1}^1 dx \left[T_g(x, \xi) F^g(x, \xi, t) + T_q(x, \xi) F^{q,S}(x, \xi, t) \right],$$

$$F^{q,S}(x, \xi, t) = \sum_{q=u,d,s} F^q(x, \xi, t).$$

where m is a pole mass of heavy quark, $\langle O_1 \rangle_V$ is given by NRQCD through leptonic meson decay rate.

Heavy Vector Mesons Photoproduction

We have good data! See H1 2013 paper:



Photoproduction cross section - LO and NLO

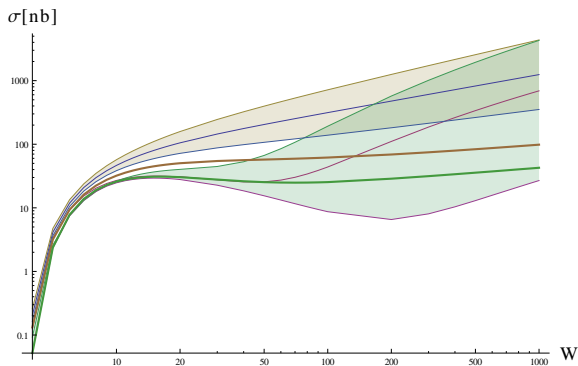
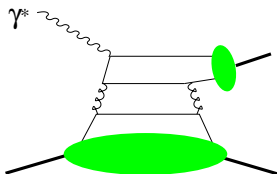
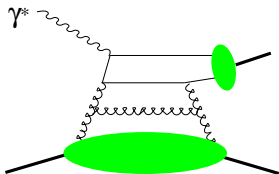


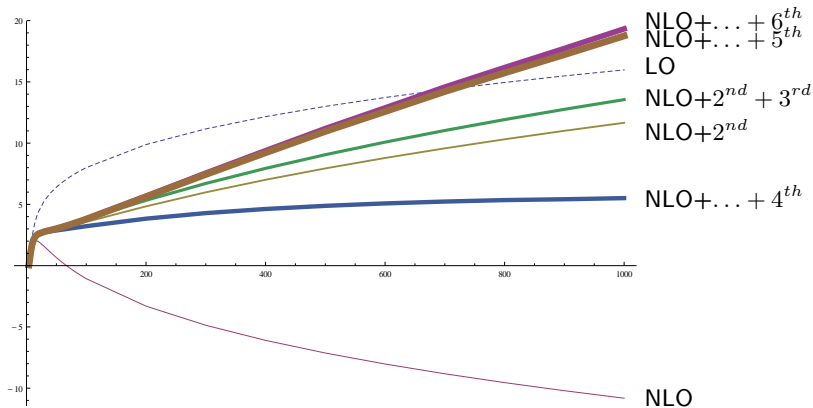
Figure: Photoproduction cross section as a function of $W = \sqrt{s_{\gamma p}}$ for $\mu_F^2 = M_{J/\psi}^2 \times \{0.5, 1, 2\}$ - LO and NLO. Thick lines for LO and NLO for $\mu_F^2 = 1/4 M_{J/\psi}^2$.

- Jones & Martin & Ryskin & Teubner, arXiv:1507.06942. Choice of the factorization scale.
- Why NLO corrections are large at small x_B ?
large contribution comes from

$$ImA^g \sim H^g(\xi, \xi) + \frac{3\alpha_s}{\pi} \left[\log \frac{M_V^2}{\mu_F^2} - \log 4 \right] \int_{\xi}^1 \frac{dx}{x} H^g(x, \xi)$$

$H^g(x, \xi) \sim xg(x) \sim const$, therefore $\int dx/x H^g(x, \xi) \sim \log(1/\xi) H^g(\xi, \xi)$





Imaginary part of the amplitude for photoproduction of heavy mesons as a function of $W = \sqrt{s_{\gamma p}}$ for $\mu_F^2 = M_{J/\psi}^2$

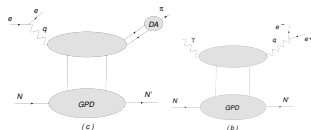
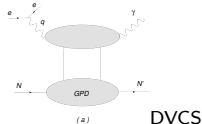


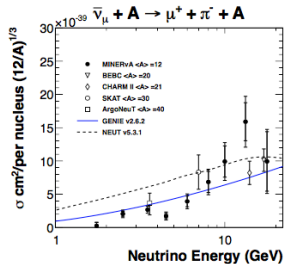
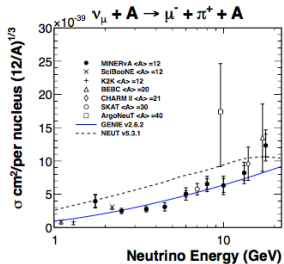
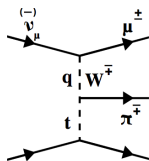
Figure: DVMP and TCS

- Various exclusive processes give information about GPDs: DVCS, TCS, DDVCS, DVMP, HVMP
- Also neutrino production of light mesons considered: allows for flavour separation, different combination of GPDs due to the charged current coupling structure. Smaller cross sections, less intense beams but process in the reach of the i.e. MINERVA experiments
→ [Kopeliovich, Schmidt, Siddikov] PRD 86

Neutrino production of charmed meson

MINERvA (Fermilab)

ν on nuclei, $E_\nu = 1 - 10$ GeV



from PRL 113, 261802 (2014) Measurement of Coherent Production of π^\pm in Neutrino and Anti-Neutrino Beams on Carbon from E_ν of 1.5 to 20 GeV

- Here we consider D pseudo scalar charmed meson production - heavy quark production allows to extend the range of validity of collinear factorization, the heavy quark mass playing the role of the hard scale.
- Factorization theorem with HEAVY quark: \rightarrow [J. C. Collins, PRD58]
 - Independently of the relative sizes of the heavy quark masses and Q
 - Size of the errors is a power of $\Lambda/\sqrt{Q^2 + M_D^2}$ when $\sqrt{Q^2 + M_D^2}$ is the large scale.
- Sensitivity to transversity GPDs. \rightarrow [Pire,Szymanowski] PRL 115

- The transverse spin structure of the nucleon - that is the way quarks and antiquarks spins share the polarization of a nucleon, when it is polarized transversely to its direction of motion - is almost completely unknown. Poorly known PDF, TMDs, GPDs.
- Lattice result and SIDIS analysis suggest that transversity distributions are not small
- Transversity GPDs coupled to chiral-odd twist 3 pi-meson DA may explain π electroproduction data at JLab [Goloskokov, Kroll], [Ahmad, Goldstein, Liuti]
- One can consider a 3-body final state process [Ivanov, Pire, Szymanowski, Teryaev], [Enberg, Pire, Szymanowski], [El Beiyad et al.], [Boussarie, Pire, Szymanowski, Wallon]

→ Leading twist process

$$\gamma N \rightarrow \rho \rho N'$$

$$\gamma N \rightarrow \pi \rho N'$$

$$\gamma N \rightarrow \gamma \rho N'$$

Neutrino-production of charmed meson

We consider the exclusive production of a pseudoscalar D -meson through the reactions on a proton (p) or a neutron (n) target:

$$\begin{aligned}\nu_l(k)p(p_1) &\rightarrow l^-(k')D^+(p_D)p'(p_2), \\ \nu_l(k)n(p_1) &\rightarrow l^-(k')D^+(p_D)n'(p_2), \\ \nu_l(k)n(p_1) &\rightarrow l^-(k')D^0(p_D)p'(p_2), \\ \bar{\nu}_l(k)p(p_1) &\rightarrow l^+(k')D^-(p_D)p'(p_2), \\ \bar{\nu}_l(k)p(p_1) &\rightarrow l^+(k')\bar{D}^0(p_D)n'(p_2), \\ \bar{\nu}_l(k)n(p_1) &\rightarrow l^+(k')D^-(p_D)n'(p_2),\end{aligned}$$

in the kinematical domain where collinear factorization leads to a description of the scattering amplitude in terms of nucleon GPDs and the D -meson distribution amplitude, with the hard subprocesses:

$$W^+d \rightarrow D^+d \quad , \quad W^+d \rightarrow D^0u \quad , \quad W^-\bar{d} \rightarrow D^-\bar{d} \quad , \quad W^-\bar{d} \rightarrow \bar{D}^0\bar{u} \quad ,$$

convoluted with **chiral-even** or **chiral-odd quark** GPDs, and the hard subprocesses:

$$W^+g \rightarrow D^+g \quad , \quad W^-g \rightarrow D^-g \quad ,$$

convoluted with **gluon** GPDs.

Feynman diagrams

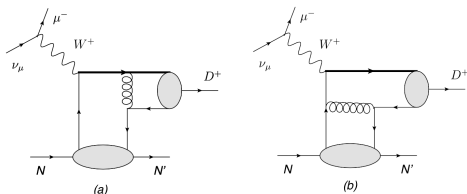


Figure: Feynman diagrams for the factorized amplitude for the $\nu_\mu N \rightarrow \mu^- D^+ N'$ process; the thick line represents the heavy quark.

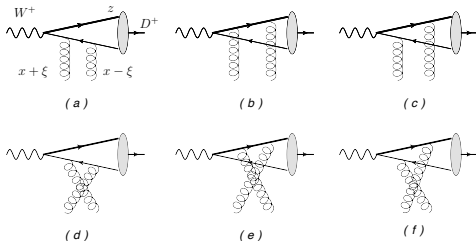


Figure: Feynman diagrams for the factorized amplitude for the $W^+ N \rightarrow D^+ N'$ process involving the gluon GPDs; the thick line represents the heavy quark.

Neutrino-production of charmed meson

Standard notations of deep exclusive leptonproduction:

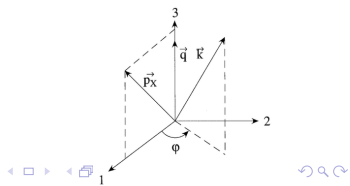
- $P = \frac{(p_1+p_2)}{2}$, $\Delta = p_2 - p_1$, $t = \Delta^2$, $x_B = \frac{Q^2}{2p_1 \cdot q}$,

- $y = \frac{p_1 \cdot q}{p_1 \cdot k}$ and $\epsilon \simeq 2(1-y)/[1+(1-y)^2]$.

- n are light-cone vectors and $\xi = -\frac{\Delta \cdot n}{2P \cdot n}$ is the skewness variable.

- The azimuthal angle φ is defined in the initial nucleon rest frame as:

$$\sin \varphi = \frac{\vec{q} \cdot [(\vec{q} \times \vec{p}_D) \times (\vec{q} \times \vec{k}_\nu)]}{|\vec{q}| |\vec{q} \times \vec{p}_D| |\vec{q} \times \vec{k}_\nu|},$$



- $\nu N \rightarrow \mu^- D^+ N$ differential cross section:

$$\frac{d^4\sigma(\nu N \rightarrow l^- N' D)}{dy dQ^2 dt d\varphi} = \tilde{\Gamma} \left\{ \frac{1 + \sqrt{1 - \varepsilon^2}}{2} \sigma_{--} + \varepsilon \sigma_{00} + \sqrt{\varepsilon}(\sqrt{1 + \varepsilon} + \sqrt{1 - \varepsilon})(\cos \varphi \operatorname{Re} \sigma_{-0} + \sin \varphi \operatorname{Im} \sigma_{-0}) \right\},$$

with

$$\tilde{\Gamma} = \frac{G_F^2}{(2\pi)^4} \frac{1}{32y} \frac{1}{\sqrt{1 + 4x_B^2 m_N^2 / Q^2}} \frac{1}{(s - m_N^2)^2} \frac{Q^2}{1 - \varepsilon},$$

and the “cross-sections” $\sigma_{lm} = \epsilon_l^{*\mu} W_{\mu\nu} \epsilon_m^\nu$ are product of amplitudes for the process $W(\epsilon_l)N \rightarrow DN'$, averaged (summed) over the initial (final) hadron polarizations.

- transverse amplitude $W_{Tq} \rightarrow Dq'$ gets its leading term in the collinear QCD framework as a convolution of chiral odd leading twist GPDs with a coefficient function of order $\frac{m_c}{Q^2}$ or $\frac{M_D}{Q^2}$ (to be compared to the $O(\frac{1}{Q})$ longitudinal amplitude)

- Chiral even GPDs: Goloskokov-Kroll model
- Transversity GPDs

$$\begin{aligned} & \frac{1}{2} \int \frac{dz^-}{2\pi} e^{ixP^+z^-} \langle p_2, \lambda' | \bar{\psi}(-\frac{1}{2}z) i\sigma^{+i} \psi(\frac{1}{2}z) | p_1, \lambda \rangle \Big|_{z^+ = z_T = 0} \\ &= \frac{1}{2P^+} \bar{u}(p_2, \lambda') \left[H_T^q i\sigma^{+i} + \tilde{H}_T^q \frac{P^+ \Delta^i - \Delta^+ P^i}{m_N^2} \right. \\ & \quad \left. + E_T^q \frac{\gamma^+ \Delta^i - \Delta^+ \gamma^i}{2m_N} + \tilde{E}_T^q \frac{\gamma^+ P^i - P^+ \gamma^i}{m_N} \right] u(p_1, \lambda). \end{aligned}$$

The GPD $H_T(x, \xi, t)$ is equal to the transversity PDF in the $\xi = t = 0$ limit. G-K provide parametrization (with some lattice input) for $H_T(x, \xi, t)$ and for the combination $\bar{E}_T(x, \xi, t) = 2\tilde{H}_T(x, \xi, t) + E_T(x, \xi, t)$. Since $\bar{E}_T(x, \xi, t)$ is odd under $\xi \rightarrow -\xi$, most models find it vanishingly small. We will put it to zero. We consider 3 models:

- model 1 : $\tilde{H}_T(x, \xi, t) = 0$; $E_T(x, \xi, t) = \bar{E}_T(x, \xi, t)$.
- model 2 : $\tilde{H}_T(x, \xi, t) = H_T(x, \xi, t)$; $E_T(x, \xi, t) = \bar{E}_T(x, \xi, t) - 2H_T(x, \xi, t)$.
- model 3 : $\tilde{H}_T(x, \xi, t) = -H_T(x, \xi, t)$; $E_T(x, \xi, t) = \bar{E}_T(x, \xi, t) + 2H_T(x, \xi, t)$.

- Usual heavy-light meson DA reads :

$$\langle D^+(P_D) | \bar{c}_\beta(y) d_\gamma(-y) | 0 \rangle = i \frac{f_D}{4} \int_0^1 dz e^{i(z-\bar{z})P_D \cdot y} [(\hat{P}_D - M_D)\gamma^5]_{\gamma\beta} \phi_D(z),$$

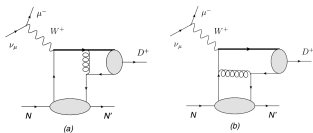
with $z = \frac{k^+}{P_D^+}$, $\int_0^1 dz \phi_D(z) = 1$, $f_D = 0.223 \text{ GeV}$, $\bar{z} = 1 - z$ and $\hat{p} = p_\mu \gamma^\mu$.

- We will parametrize $\phi_D(z)$:

$$\phi_D(z) = 6z(1-z)(1 + C_D(2z-1))$$

with $C_D \approx 1.5$, which has a maximum around $z = 0.7$.

→ [T. Kurimoto, H. n. Li and A. I. Sanda, Phys. Rev. D 65]



The transverse amplitude is then written as ($\tau = 1 - i2$):

$$T_T = \frac{-i2C_q \xi (2M_D - m_c)}{\sqrt{2}(Q^2 + M_D^2)}$$

$$\bar{N}(p_2) \left[\mathcal{H}_T i\sigma^{n\tau} + \tilde{\mathcal{H}}_T \frac{\Delta^\tau}{m_N^2} + \mathcal{E}_T \frac{\hat{n}\Delta^\tau + 2\xi\gamma^\tau}{2m_N} - \tilde{\mathcal{E}}_T \frac{\gamma^\tau}{m_N} \right] N(p_1),$$

with $C_q = \frac{2\pi}{3} C_F \alpha_s V_{dc}$, in terms of transverse form factors that we define as :

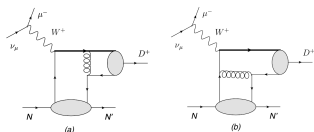
$$\mathcal{F}_T = f_D \int \frac{\phi_D(z) dz}{\bar{z}} \int \frac{F_T^d(x, \xi, t) dx}{(x - \xi + \beta\xi + i\epsilon)(x - \xi + \alpha\bar{z} + i\epsilon)},$$

where F_T^d is any d-quark transversity GPD, $\alpha = \frac{2\xi M_D^2}{Q^2 + M_D^2}$, $\beta = \frac{2(M_D^2 - m_c^2)}{Q^2 + M_D^2}$.

- T_T vanishes when $m_c = 0 = M_D$.

For chiral-even GPDs due to the collinear kinematics and the leading twist CF

For chiral-odd GPDs due to the odd number of γ matrices in the Dirac trace.



The quark contribution to longitudinal amplitude of leading twist is a slight modification of the calculation in:

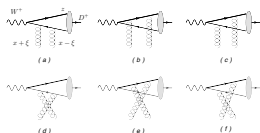
B. Z. Kopeliovich, I. Schmidt and M. Siddikov, Phys. Rev. D **86** and D **89**
 G. R. Goldstein, O. G. Hernandez, S. Liuti and T. McAskill, AIP Conf. Proc. **1222**

$$T_L^q = \frac{-iC_q}{2Q} \bar{N}(p_2) \left[\mathcal{H}_L \hat{n} - \tilde{\mathcal{H}}_L \hat{n} \gamma^5 + \mathcal{E}_L \frac{i\sigma^{n\Delta}}{2m_N} - \tilde{\mathcal{E}}_L \frac{\gamma^5 \Delta \cdot n}{2m_N} \right] N(p_1),$$

with the chiral-even form factors defined by

$$\mathcal{F}_L = f_D \int \frac{\phi_D(z) dz}{\bar{z}} \int dx \frac{F^d(x, \xi, t)}{x - \xi + \alpha \bar{z} + i\epsilon} \left[\frac{x - \xi + \gamma \xi}{x - \xi + \beta \xi + i\epsilon} + \frac{Q^2}{Q^2 + z M_D^2} \right],$$

$$\text{with } \gamma = \frac{2M_D(M_D - 2m_c)}{Q^2 + M_D^2}, \quad \beta = \frac{2(M_D^2 - m_c^2)}{Q^2 + M_D^2}$$



The **gluonic** contribution to the amplitude reads:

$$\begin{aligned}
 T_L^g &= \frac{iC_g}{2} \int_{-1}^1 dx \frac{-1}{(x+\xi-i\epsilon)(x-\xi+i\epsilon)} \int_0^1 dz f_D \phi_D(z) \cdot \\
 &\quad \left[\bar{N}(p_2) \left[H^g \hat{n} + E^g \frac{i\sigma^{n\Delta}}{2m} \right] N(p_1) \mathcal{M}_H^S \right. \\
 &\quad \left. + \bar{N}(p_2) \left[\tilde{H}^g \hat{n} \gamma^5 + \tilde{E}^g \frac{\gamma^5 n \cdot \Delta}{2m} \right] N(p_1) \mathcal{M}_H^A \right] \\
 &\equiv \frac{-iC_g}{2Q} \bar{N}(p_2) \left[\mathcal{H}^g \hat{n} + \mathcal{E}^g \frac{i\sigma^{n\Delta}}{2m} + \tilde{\mathcal{H}}^g \hat{n} \gamma^5 + \tilde{\mathcal{E}}^g \frac{\gamma^5 n \cdot \Delta}{2m} \right] N(p_1),
 \end{aligned}$$

where the last line defines the gluonic form factors \mathcal{H}^g , $\tilde{\mathcal{H}}^g$, \mathcal{E}^g , $\tilde{\mathcal{E}}^g$ and $C_g = T_f \frac{\pi}{3} \alpha_s V_{dc}$ with $T_f = \frac{1}{2}$ and the factor $\frac{-1}{(x+\xi-i\epsilon)(x-\xi+i\epsilon)}$ comes from the conversion of the strength tensor to the gluon field.

The longitudinal cross section σ_{00}

$$\sigma_{00} = \frac{1}{Q^2} \left\{ \begin{aligned} & [|C_q \mathcal{H}_L + C_g \mathcal{H}_g|^2 + |C_q \tilde{\mathcal{H}}_L - C_g \tilde{\mathcal{H}}_g|^2] (1 - \xi^2) \\ & + \frac{\xi^4}{1 - \xi^2} [|C_q \tilde{\mathcal{E}}_L - C_g \tilde{\mathcal{E}}_g|^2 + |C_q \mathcal{E}_L + C_g \mathcal{E}_g|^2] \\ & - 2\xi^2 \text{Re} [C_q \mathcal{H}_L + C_g \mathcal{H}_g] [C_q \mathcal{E}_L^* + C_g \mathcal{E}_g^*] \\ & - 2\xi^2 \text{Re} [C_q \tilde{\mathcal{H}}_L - C_g \tilde{\mathcal{H}}_g] [C_q \tilde{\mathcal{E}}_L^* - C_g \tilde{\mathcal{E}}_g^*] \end{aligned} \right\}.$$

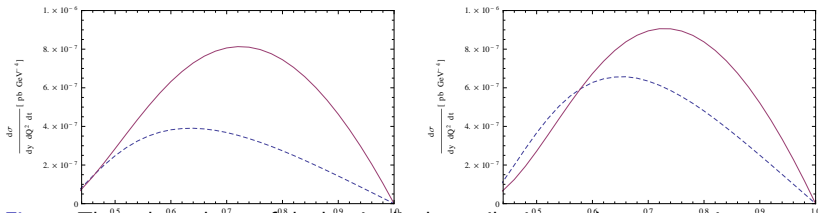


Figure: The y dependence of the longitudinal contribution to the cross section $\frac{d\sigma(\nu N \rightarrow l^- ND^+)}{dy dQ^2 dt}$ (in pb GeV^{-4}) for $Q^2 = 1 \text{ GeV}^2$, $\Delta_T = 0$ and $s = 20 \text{ GeV}^2$ for a proton (left panel) and neutron (right panel) target : total (quark and gluon, solid curve) and quark only (dashed curve) contributions. **GLUONS IMPORTANT!!!**

The transverse cross section σ_{--}

$$\sigma_{--} = \frac{16\xi^2 C_q^2 (m_c - 2M_D)^2}{(Q^2 + M_D^2)^2} \left\{ (1 - \xi^2) |\mathcal{H}_T|^2 + \frac{\xi^2}{1 - \xi^2} |\mathcal{E}'_T|^2 - 2\xi \text{Re}[\mathcal{H}_T \mathcal{E}'_T^*] \right\}$$

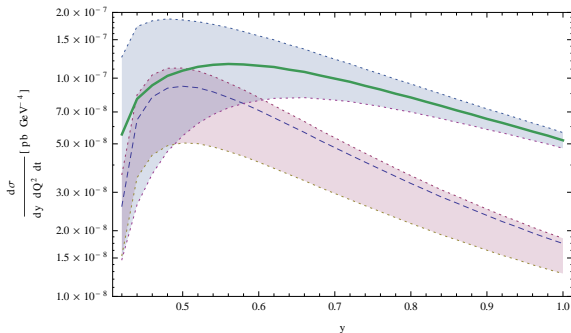


Figure: The y dependence of the transverse contribution to the cross section $\frac{d\sigma(\nu N \rightarrow l^- N D^+)}{dy dQ^2 dt}$ (in pb GeV^{-4}) for $Q^2 = 1 \text{ GeV}^2$, $\Delta_T = 0$ and $s = 20 \text{ GeV}^2$ for a proton (dashed curve) and neutron (solid curve) target.

Vanishes at zeroth order in Δ_T , the term linear in Δ_T/m_N reads

$$\lambda = \tau^* = 1 + i2$$

$$\begin{aligned} \sigma_{-0} = & \frac{\xi\sqrt{2}C_q}{m} \frac{2M_D - m_c}{Q(Q^2 + M_D^2)} \left\{ \right. \\ & - i\mathcal{H}_T^*[C_q\tilde{\mathcal{E}}_L - C_g\tilde{\mathcal{E}}_g]\xi\epsilon^{pn\Delta\lambda} + i\mathcal{E}'_T^*\epsilon^{pn\Delta\lambda}[C_q\tilde{\mathcal{H}}_L - C_g\tilde{\mathcal{H}}_g] \\ & + 2\tilde{\mathcal{H}}_T^*\Delta^\lambda\{C_q\mathcal{H}_L + C_g\mathcal{H}_g - \frac{\xi^2}{1-\xi^2}[C_q\mathcal{E}_L + C_g\mathcal{E}_g]\} \\ & + \mathcal{E}_T^*\Delta^\lambda\{(1-\xi^2)[C_q\mathcal{H}_L + C_g\mathcal{H}_g] - \xi^2[C_q\mathcal{E}_L + C_g\mathcal{E}_g]\} \\ & \left. - \mathcal{H}_T^*\Delta^\lambda[C_q\mathcal{E}_L + C_g\mathcal{E}_g] + \mathcal{E}'_T^*\Delta^\lambda\xi[C_q\mathcal{H}_L + C_g\mathcal{H}_g + C_q\mathcal{E}_L + C_g\mathcal{E}_g]\right\} \end{aligned}$$

In our kinematics, $\Delta^1 = \Delta^x = \Delta_T$, $\Delta^y = 0$, $\epsilon^{pn\Delta\lambda} = -i\Delta_T$.

$$\langle \cos \varphi \rangle = \frac{\int \cos \varphi d\varphi d^4\sigma}{\int d\varphi d^4\sigma} = K_\epsilon \frac{\text{Re}\sigma_{-0}}{\sigma_{00}},$$

$$\langle \sin \varphi \rangle = K_\epsilon \frac{\text{Im}\sigma_{-0}}{\sigma_{00}}$$

- with $K_\epsilon = \frac{\sqrt{1+\epsilon} + \sqrt{1-\epsilon}}{2\sqrt{\epsilon}}$
- Simple approximate results:

$$\langle \cos \varphi \rangle \approx \frac{K \text{Re}[\mathcal{H}_D(2\tilde{\mathcal{H}}_T^\phi + \mathcal{E}_T^\phi + \bar{\mathcal{E}}_T^\phi)^* - \mathcal{E}_D \mathcal{H}_T^{\phi*}]}{8|\mathcal{H}_D^2| + |\tilde{\mathcal{E}}_D^2|},$$

$$\langle \sin \varphi \rangle \approx \frac{K \text{Im}[\mathcal{H}_D(2\tilde{\mathcal{H}}_T^\phi + \mathcal{E}_T^\phi + \bar{\mathcal{E}}_T^\phi)^* - \mathcal{E}_D \mathcal{H}_T^{\phi*}]}{8|\mathcal{H}_D^2| + |\tilde{\mathcal{E}}_D^2|},$$

$$K = -\frac{\sqrt{1+\epsilon} + \sqrt{1-\epsilon}}{2\sqrt{\epsilon}} \frac{2\sqrt{2}\xi m_c}{Q} \frac{\Delta_T}{m_N}$$

Azimuthal dependence

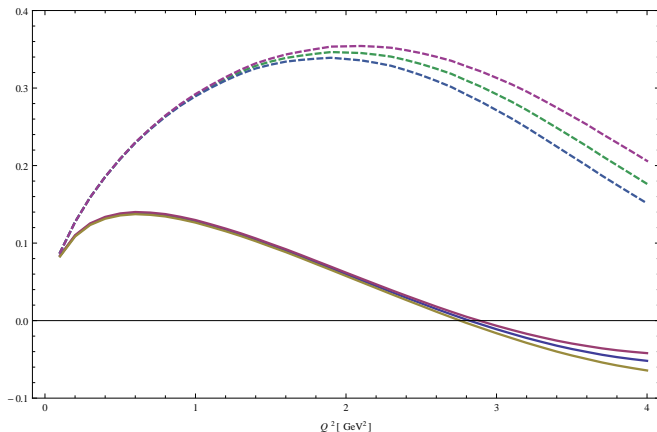


Figure: The Q^2 dependence of the $\langle \cos \varphi \rangle$ (solid curves) and $\langle \sin \varphi \rangle$ (dashed curves) moments normalized by the total cross section, for $\Delta_T = 0.5$ GeV, $y = 0.7$ and $s = 20$ GeV². The three curves correspond to the three models explained in the text, and quantify the theoretical uncertainty of our estimates.

Light meson production - importance of gluon contribution.

J. Wagner, B. Pire, LSz in preparation

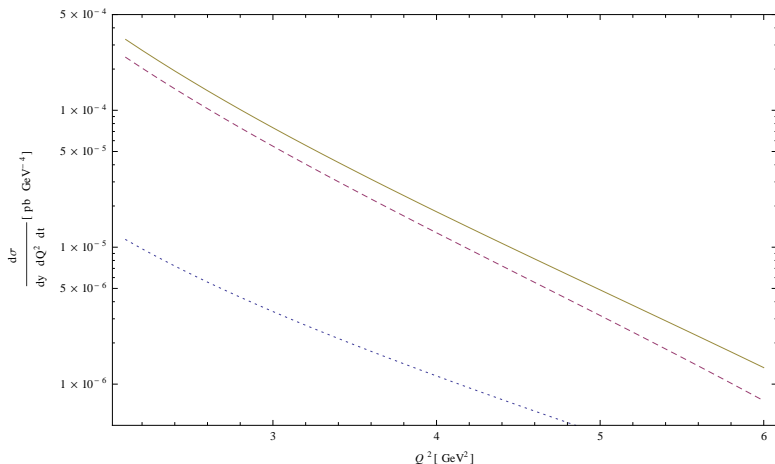


Figure: The Q^2 dependence of the quark (dashed curve) contribution compared to the total (quark and gluon, solid curve) longitudinal cross section $\frac{d\sigma(\nu N \rightarrow l^- N \pi^+)}{dy dQ^2 dt}$ (in pb GeV $^{-4}$) for π^+ production on a proton target for $y = 0.7$, $\Delta_T = 0$ and $s = 20$ GeV 2 .

- Collinear QCD factorization allows to calculate neutrino production of D -mesons in terms of GPDs down to $Q^2 = 0$.
- Chiral-odd and chiral-even GPDs contribute to the amplitude for different polarization states of the W
- The azimuthal dependence of the cross section allows to get access to chiral-odd GPDs
most sensitive for transversity GPD is $\bar{\nu} p \rightarrow l^+ \bar{D}^0 n$
- The behaviour of the proton and neutron target cross sections for D^+ , D^- and D^0 production with ν and $\bar{\nu}$ enables to separate the u and d quark contributions.
- Within the reach of planned medium and high energy neutrino facilities and experiments such as MINER ν A and MINOS+.
- Gluon contribution very important \rightarrow consequences for light mesons!